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Molecular dynamics simulation of peptide folding

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Abstract The simulation of peptide folding with atomic resolution has evolved remarkably during the last 7 years, i.e., from absolute skepticism on the capability of classical molecular dynamics (MD) methodology to reproduce complex biological phenomena such as the folding of even simple oligopeptides (6–15 residues) to the seemingly realistic representation of the thermodynamics and kinetics of folding of a rapidly increasing number of polypeptides (over 20 residues). Four factors permitted this rapid progress: the breakthrough of a second generation of force fields, a rapid and steady increase of (commodity) computer performance, a move from local computational resources to large distributed clusters and, last but not less important, a decision of particular groups to spend a large computational effort on projects that most other groups trusted unrealizable at the time. The present account goes over some aspects of peptide folding and its simulation with MD techniques while sweeping through the simulation landmarks of the last 7 years and conjecturing on the future.

1 Introduction

Peptide chains exist in an equilibrium between different conformations as a function of environment – number of molecules for each of the molecular species present in the system – and thermodynamic – temperature, pressure – conditions. If a peptide adopts a structurally ordered, densely populated conformation, it is commonly said to have a folded state, identified with this conformer, in equilibrium with the unfolded state, represented by diverse, sparsely populated conformers. Although, in principle, this equilibrium exists for chains of

any size, its thermodynamics and kinetics are typically different for oligopeptides forming secondary structure elements, polypeptides (over 20 residues) with some degree of tertiary structure and proteins (over 50 residues) with a substantial solvent-excluded volume (hydrophobic core). This can be broadly explained with reference to the different dimensionalities of the free enthalpy hypersurfaces of these three classes of polymers of amino acids.

Historically, research on peptide and protein structure, whether by experimental or computational means, has focused on the folded state only. This is because an array of methods exists for the detailed investigation of the folded state of a peptide or protein, and because the folded state is commonly the functionally active one. There are, however, two scenarios in which a full characterization of the unfolded state becomes as essential as the determination of the folded conformation. The first is in the study of the physical, chemical, or biological properties of oligopeptides and short polypeptides. The folded conformation of such peptides is, in general, only marginally more stable than the lowest free enthalpy unfolded conformation. Moreover, the unfolded state of a peptide is often more populated than the folded state. As a result, any macroscopic observable of a peptide is weighted with both the folded and the unfolded states. Interpreting such observables in terms of only the folded conformation is, therefore, incorrect. The second scenario is related to the study of peptide and protein folding (to be distinguished from structure prediction). The description of an equilibrium requires knowledge about each of the states involved. Therefore, it is fundamental to describe not only the folded state but also the unfolded state accurately in order to draw conclusions on the nature and mechanisms of peptide and protein folding.

More recently, some efforts have been made to characterize the unfolded state of specific peptides and proteins [1–16]. Obtaining quantitative microscopic information from the unfolded state is difficult not only experimentally but also computationally. While experiments suffer from the low population and transient nature of individual unfolded conformations, theoretical studies are bound by the computational time required to sample the conformations of the unfolded state

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with appropriate weights. In most cases, experimental studies report on low-resolution average properties of the unfolded state [4,6,8,13–15] or focus on particular, not always well-defined substates like, for example, molten globules [17–19], metastable intermediates [20], or transition states [21–26], (see also reviews [27–31] and *Adv Prot Chem*, vol 62 on *Unfolded Proteins*). Computationally, sampling the unfolded state is bound to sampling the equilibrium ensemble of folding/unfolding pathways. Given the size of the problem, the challenge is to reduce the number of degrees of freedom of the model without perturbing its capacity to reproduce the behavior of the real system. The number of degrees of freedom can be kept to a computationally tractable number by either simplifying the physical model for the protein and/or its environment [32–43], or limiting the size of the molecular system to that of atomic-detail models of oligo- and polypeptides in solution [44–51]. Alternatively, for an atomic-detail model of a protein in solution, if the native three-dimensional structure is known one may construct a projection of the free enthalpy on particular coordinates using a predefined set of unfolded conformations and biased-sampling [52], or one may perform unfolding simulations under denaturing conditions and assume that the sampled pathways are relevant to folding under native conditions [53]. Arguments in favor and against each of these simplifying approaches are abundant in the mentioned literature.

The focus of this paper is on the molecular dynamics (MD) simulation of oligo- and polypeptide folding with atomic resolution.

2 1998–2005: Simulation landmarks

Although the simulation of peptide dynamics has already a long trajectory [54,55], before 1998 it was generally accepted that the folding of even small oligopeptides forming secondary structure elements – helices and hairpins – could not be tackled with MD simulation methods [56]. Reasons for this skepticism were the estimated timescales of folding, far beyond the computationally accessible timescales at the time, and the general feeling that the empirical force fields and other approximations intrinsic to MD simulation meant that this methodology would not be, in the foreseeable future, applicable to complex phenomena like folding.

Around 1997, however, the groups of van Gunsteren and Kollman made significant advances with somewhat different approaches. In the immediately preceding years, second generations of the most widely used force fields for biomolecular simulation had been developed [57–60]. In addition, it had become apparent that the experimentally estimated folding times depended strongly on the resolution of the technique used as well as on the model applied to interpret the data, and that actual folding times could well be shorter than estimated. Studying the structural properties of a synthetic β -peptide in methanol at different temperatures, Daura et al. [61] observed, as a matter of chance, the unfolding and refolding of the experimentally determined left-handed helix

at high temperature in a short simulation. This observation encouraged the authors to attempt an extensive study of the conformational behavior of the peptide at a range of temperatures over a timescale of 50 ns, an order of magnitude larger than common simulations of the time [44]. The results of this study demonstrated, for the first time, that the MD technique could be used to simulate not only the folding of a peptide but also the equilibrium between the unfolded and folded states, with the root mean square difference (RMSD) between the backbones of the NMR model and the helix populated in the simulations being as low as 0.02 nm. Certainly, neither the peptide nor the solvent were biologically relevant, but there was nothing in the methods or the force field that could make the folding of an α -peptide in water less tractable, the physical principles being the same. This was shortly after a demonstration by Duan and Kollman [45], who had taken a complementary approach. They attempted the folding of a 36-residue polypeptide, villin headpiece subdomain, in water with a phenomenally long (1 μ s) simulation. The lower bound to the folding time of this polypeptide had been estimated in 10 μ s (current estimates are around 5 μ s [62]). Nevertheless, the most populated conformer in the simulation contained many of the features of the NMR model structure and the authors suggested that it could correspond to a metastable folding intermediate. This simulation time record (still the longest continuous simulation of a polypeptide in explicit solvent to date) could be achieved thanks to the use of large supercomputing resources, an optimized parallel code developed by the same authors, and a reduced box size in combination with a simplified long-range interaction scheme. The papers by Daura et al. [44] and Duan and Kollman [45] showed that the simulation of the folding of small proteins with atomic resolution was not a chimera but, rather, a question of time [63]. The difficulty to access large supercomputing resources meant that, in most cases, the study of peptide folding by MD simulation was approached from extensive simulations aimed at reproducing the folding/unfolding equilibrium of small, quick folders (oligopeptides) [46,48,64–66].

In late 1998, a paper by Schaefer et al. [67] opened new expectations on a long-debated simplifying approach, i.e., the use of (improved) implicit-solvent representations in biomolecular simulation in general and in peptide folding in particular. This level of modeling permitted a significant timescale jump and was quickly adopted by a number of groups studying peptide folding [38,68–72]. (Interestingly, it did not have a comparable impact on MD simulations of folded proteins.) In particular, Ferrara et al. [37,73] used this fast approach to improve folding statistics with multiple long simulations. The presumed correspondence between implicit- and explicit-solvent thermodynamics and kinetics is, however, a matter of active discussion [74–83].

In parallel to these developments, two papers prepared the terrain for two future important lines of work. On the one hand, Sugita and Okamoto [84] developed a formulation for replica-exchange MD. This built on the replica [85] and multicanonical [86] Monte Carlo algorithms, the latter having been already adapted to MD [87] and later used in peptide

folding simulations [47]. In replica-exchange MD, system replicas at different temperatures (over a defined range) are run simultaneously and independently. Every so many steps, a pair of replicas at neighboring temperatures are exchanged with a Metropolis-based probability. The algorithm permits an efficient sampling of conformational space with appropriate weights. On the other hand, Voter [88] proposed a parallel-replica MD algorithm for efficient parallelization (minimal communication between nodes) of the simulation of rare events. A (large) number of replicas are also run in parallel, with different initial conditions (randomized momenta). When one of the replicas makes a transition to another state, all the replicas are reset to that state. The algorithm preserves the right kinetics. The door to (commodity) distributed computing was open.

In 2001, García and Sanbonmatsu [49] applied the replica-exchange MD algorithm to the study of peptide folding. Since then, this method and its derivatives [89–92] have become standards for the study of peptide-folding thermodynamics, both in explicit- and implicit-solvent environments [93–97]. Although the method allows a very efficient sampling of conformational space, effectively crossing over barriers, it does not lack inconveniences. Thus, the kinetics are scrambled by the exchange procedure and, in explicit solvent, efficient exchange requires in general the use of constant volume and a small spacing between temperatures, i.e., many replicas. Distinct formalisms, with derivations based to a varying extent on Markov chains, have been already proposed for the recovery of kinetic information on a system by reusing a Boltzmann-weighted distribution of states (e.g., from replica-exchange simulations) [98–100].

Building on previous efforts to apply large-scale distributed computing to biomolecular simulation [88, 101, 102], in 2002 Snow et al. [50] reported a kinetic study of the folding of a 23-residue polypeptide in implicit solvent by multiple, tens of thousands, relatively short MD simulations, using parallel-replica MD. As impressive as it is, this approach is neither without problems. The thermodynamics of the system are biased and the ability of the approach to evaluate the folding kinetics of proteins, as opposed to peptides, has been questioned [103] (although a kinetic model that could potentially circumvent this problem has been already proposed [104]). In addition, the complex infrastructure/logistics required by this approach means that only one group is actively using it at the moment [105].

3 A view on peptide folding

Looking at the existing literature, an outsider would easily conclude that the knowledge on how peptides fold is extense. A myriad of seemingly consistent conclusions have been written down, some compatible some not, most of them defensible but few irrefutable or generalizable. Indeed, there have been many interpretations of peptide folding on the basis of experimental and theoretical data, but there is still little true knowledge. Even when detailed computational models

seem to reproduce accurately the experimental data, offering a plausible microscopic picture of the process, it is difficult to interpret the trajectories without introducing yet more models and assumptions in the analysis.

In the following paragraphs I will treat some aspects of peptide folding, mostly in connection with our own work. A significant part of our experience is based on observations from MD simulations of the reversible folding of non-natural peptides (especially β -peptides [106]) in non-aqueous solvents [7, 107]. Whether results on these systems can be extrapolated to natural peptides in water is, of course, questionable. As a matter of fact, Kritzer et al. [108] have recently suggested that β -peptide folding might be governed by different biophysical forces than α -peptide folding. Finally, note that protein folding does not necessarily proceed as a simple extension of peptide folding, and I will only refer to the latter process.

3.1 The framework

I will start by defining unambiguously, though in some cases arbitrarily, some terminology. *Configuration* will be used to describe a set of distinct coordinates of the atoms of a molecular system. *Structure* will be used to describe a set of distinct internal coordinates of the atoms of a peptide. *Conformation*, on the other hand, will be used as an abstraction representing an (in principle infinite) ensemble of structures of a peptide with high structural similarity and identical macroscopic properties. From these definitions it follows that the *configurational space* (continuous) of a peptide is infinite, while the *conformational space* (discrete) is not. The term *accessible conformational space* will be based on thermodynamics rather than kinetics. Thus, it will refer to the space of likely conformations, conformations with non-zero probability, at equilibrium.

Consider a peptide in conformational equilibrium. Suppose the peptide is part of a microscopic system in contact with a reservoir at constant temperature and pressure (exchange of heat and work). The conformational space accessible to the peptide (and its associated probability distribution) depends on the rest of the system or environment, **E**, and the thermodynamic conditions, **C**. I will call the most probable conformation of the peptide under **E,C** the *folded conformation* of the peptide. Any other conformers populated under **E,C** will be said to be *unfolded*. Note that this is irrespective of structural considerations, i.e., the most probable conformer may or may not be recognized as a secondary structure element, while there might be lower probability (unfolded) conformers recognizable as canonical secondary structures. In addition, the folded conformer is not necessarily unique, as it may change with **E,C**. The terms *state* and *free enthalpy* (or Gibbs free energy) refer to the system. Thus, the *folded state* under **C** is here defined as the ensemble of microstates of the system, states with specified atomic coordinates and momenta for all atoms, for which the peptide is in its folded conformation, while the *unfolded state* under **C**

is defined by all other microstates populated by the system. Likewise, I may define system states associated to each of the unfolded conformations of the peptide. For simplicity, I will use the term *conformational state* to refer to a system state associated to a particular conformation of the peptide. Using this nomenclature, the free enthalpy difference between any pair AB of states (e.g., free enthalpy of folding if A is the unfolded state and B the folded state) under \mathbf{C} is given by:

$$\Delta G_{AB}^{(\mathbf{C})} = -\beta^{-1} \ln \left[P_B^{(\mathbf{C})} / P_A^{(\mathbf{C})} \right], \quad (1)$$

where $\beta = (k_B T)^{-1}$, k_B is the Boltzmann constant, T is the temperature, and $P_X^{(\mathbf{C})}$ is the probability of state X under \mathbf{C} :

$$P_X^{(\mathbf{C})} = \frac{\sum_i P_{X_i}^{(\mathbf{C})} e^{-\beta H_{X_i}^{(\mathbf{C})}}}{\sum_Y \sum_j e^{-\beta H_{Y_j}^{(\mathbf{C})}}}, \quad (2)$$

with $H_{X_i}^{(\mathbf{C})}$ being the enthalpy of microstate X_i , belonging to state X , under \mathbf{C} . Note that the sum over all conformational states Y (partition function) in Eq. (2) vanishes in Eq. (1). Note also that in principle the sums over microstates i, j in Eq. (2) are integrals over phase space. However, the impossibility to specify a microstate, a point in phase space, with infinite accuracy (theoretically) and precision (computationally) means that the phase space of the system is, for our purposes, discrete and we may approach these integrals as sums. The sum over microstates of the Boltzmann factor $e^{-\beta H_{X_i}^{(\mathbf{C})}}$ is very hard to estimate, even for a conformational state. Although only the low enthalpy microstates of X will significantly contribute to the sum, the Boltzmann factor is always positive and, therefore, we may severely underestimate the sum if any low free enthalpy microstates are missed. MD simulations are rather efficient at sampling the low enthalpy microstates, especially for rapidly relaxing environments like water. However, if the environment of the peptide contains other slowly relaxing molecular species, e.g., another peptide, in addition to the solvent, the estimation of the sum becomes impossible, as it involves the sampling of the conformational space accessible to the second peptide under the conditions that the enthalpy of the corresponding microstates is low and the first peptide is in the conformation that defines state X . Finally, the probabilities might be also estimated by population counting from an equilibrium distribution of conformational states. This is normally the approach used to analyze peptide-folding thermodynamics from simulation trajectories, the problem being again the difficulty to sample such equilibrium even for simple peptide/solvent systems. It has the basic advantage of not requiring any calculation.

For the sake of discussion, I will define yet another conformational state: the *native state*. This will be a system state associated to the experimentally observable (and biologically relevant) conformation of the peptide (native conformation), without consideration of its relative probability. By analogy to the folded/unfolded pair, I define the *denatured state* as the ensemble of populated microstates of the system for which the peptide is not in the native conformation. As with the

folded conformer, the native conformer of a peptide may not be unique but will be dependent on \mathbf{E}, \mathbf{C} . For example, the native conformation of a peptide may be different in vacuum [109–112], in aqueous solution and when inserted in a membrane.

3.2 Bounds to a conformation

The concept of conformation is necessarily ill-defined. As an abstraction of a region of the configurational space of a peptide, it has no natural bounds. Thus, any set of criteria we use to define a conformation will be unavoidably arbitrary. However, some criteria conform better to the concept than others. In MD simulation studies, the assignment of sampled structures of a peptide to particular conformations is in general done through clustering. Clustering algorithms used in the context of peptide folding are diverse in nature and mathematical complexity. More important than the algorithm, however, are the descriptors used to determine whether two structures belong to the same conformation. The most common descriptors are global measures of (backbone) structure, e.g., RMSDs of atomic positions [113] or atomic distances [114], population densities in some type of projection of the configurational space sampled [115–117], strings of dihedral angles and associated secondary structure motifs [118], etc. In some cases, a set of local descriptors has been used, e.g., particular types of atomic interactions [69], occasionally in combination with specific energy terms [119]. An approach to conformation from phase space rather than configurational space would be desirable. Huisinga et al. [120], for example, devised a dynamics-based clustering which characterizes conformations in terms of their metastability with respect to fluctuations. Although an appealing idea, this type of analysis becomes impractical for large sets.

3.3 Thermodynamics versus kinetics

The most probable state of a system is, by definition (Eq. (1)), the one with the lowest free enthalpy. An apparently naive question then rises: is the native state under \mathbf{C} the most probable state under \mathbf{C} (i.e., are the states defined here as native and folded the same)? The answer is not straightforward. For example, it is common to read (although more in relation to proteins) that the native conformation of a peptide is the conformation with the lowest free enthalpy from those which are kinetically accessible. This sentence may be confusing. First, except for a peptide in vacuum, a peptide conformation does not have an associated free enthalpy. As already mentioned, free enthalpy is a system property. Thus, it is the peptide/ \mathbf{E} system that will (eventually) evolve toward its lowest free enthalpy state and not the peptide. In addition, to define the free enthalpy of the system as a function of, say, the peptide conformation, one must first fix the thermodynamic conditions (\mathbf{C}). Second, we need to introduce the concept of kinetic inaccessibility. If a state is truly

(thermodynamically) inaccessible it will have zero probability and, hence, an infinitely high relative free enthalpy. We can argue, however, that the average life time of the system may be shorter than the minimum time it needs to reach its lowest free enthalpy conformational state and, therefore, a higher free enthalpy, kinetically more accessible, conformational state (native state) might be systematically more populated. In other words, the life time of the system may be much shorter than its relaxation time, i.e. the time required to reach an equilibrium distribution of (conformational) states. Thus, the question reduces to whether natural peptide/E systems are in equilibrium. From our (maybe still poor) understanding of the characteristics of free enthalpy landscapes of peptides in dilute solution (the particular case we are treating here) we can assume that there are no unsurmountable kinetic barriers in these landscapes and, therefore, conditions close to equilibrium may exist for naturally occurring life times. There is also a practical reason to avoid considering the possibility of non-equilibrium peptide/E systems: most available formalisms to study peptide-folding thermodynamics refer to equilibrium distributions of states. It does, in fact, make little sense to talk about probabilities and inaccessible states if the real system can never sample the conformational space with appropriate (equilibrium) weights. Hence, I will assume that what I have defined as folded and native corresponds to the same conformational state.

3.4 Accessible conformational space

It has been proposed that fast folding, i.e., folding in biologically relevant timescales, may be achieved thanks to a bias of the unfolded state toward the folded state [36,121]. This has been often expressed as a preference of the system for native contacts. Supposedly, this bias could have been introduced by some evolutionary mechanism. But, what could this bias be? The answer must be necessarily in the Hamiltonian of the system. For example, imagine a peptide/water microscopic system with the peculiarity that all atoms interact only through a very basic short-range repulsion term that avoids atomic overlap (in addition to a unique bonding term for bound atoms). The entire conformational space of the peptide would be basically accessible, and all the conformational states of the system would have similar probabilities (distinguished only entropically). In a landscape like this, finding a particular conformation and ensuring its stability during a biologically meaningful time would be a hard task. The Hamiltonian governing a real peptide/water system is obviously much more complex than this and it differentially weights conformational states, effectively reducing the conformational space accessible to the peptide. How much is the space reduced and in which direction (if a specific one) is a question of active discussion. There are indications that in the unfolded state the average structural properties of a peptide may be close to those in the folded state [10,114,122]. This is not, however, incompatible with the conformations of the peptide in the unfolded state being at the same time

structurally diverse (to be distinguished from random), with many of the populated conformers lacking native contacts [113,123–125].

Based on simulation studies of the equilibria of non-natural peptides (mostly) in non-aqueous solvents at different temperatures, we proposed that the number of conformational states accessible to a peptide is far, orders of magnitude, smaller than the number of theoretical conformational states – states resulting from the consideration of a fixed, e.g., 3, number of conformers per backbone angle – and that, opposite to the theoretical space, the accessible space does not grow exponentially with the length of the peptide [7]. In the picture that emerged from these simulations, the unfolded state is heavily dominated by a relatively small number of conformational states, and folding occurs, in average, through a small number of intermediates [107]. We suggested that there might be a correlation between the number of accessible (populated) conformational states and the average folding time [7,126] and, therefore, a conformational landscape like the one proposed would favor fast folding kinetics. We also suggested that the average life time of the folded state might grow faster with the number of residues than the average folding time, thus making folding a more efficient process for longer chains [107]. Theoretical and experimental kinetic data suggest that, for proteins, the scaling of the folding time with the number of residues (N) is roughly proportional to $e^{N^{1/2}}$ (the proportionality constant being in microseconds) [127,128]. On the other hand, the minimum folding time for a single-domain protein would be approximately $N/100 \mu\text{s}$ [129]. The dependence we observe for our reduced set of peptides is approximately linear in nature, in line with the latter fast folders (albeit with a different slope) [107]. Some aspects of our analysis of the accessible conformational space and its implications on folding have been, however, criticized. In particular, it has been argued that the average number of (unfolded) conformational states visited during folding may be small and the accessible conformational space still grow exponentially with the length of the peptide [130,131].

Currently, we are analyzing the accessible conformational spaces of two β -peptides in methanol, at different temperatures, in terms of network theory [132]. The populated conformational states are determined by clustering peptide structures sampled at regular time intervals during the simulation [113]. Each conformational state represents, thereafter, a node in the graph (network). Links between nodes correspond to bidirectional transitions between the conformational states (clusters) sampled during the simulation. Preliminary results from this analysis (R.V. Solé and X. Daura, in progress) indicate that the accessible conformational spaces of these peptides have a small-world topological organization (high clustering, small average path length) with an exponential degree distribution [most clusters can perform transitions to only one or two other clusters, whereas a few of them (hubs) have multiple connections]. Similar results have been recently reported by Rao and Caffisch [133] on a 20-residue antiparallel β -sheet peptide. This level of organization, which agrees with our previous observation of a small

average number of folding intermediates, explains to a large degree the fast folding of these so-called foldamers.

3.5 Specific folding energetics

For one of these peptides, the energetics have been analyzed using classical thermodynamics formulae that relate free enthalpy and entropy differences over a temperature range to enthalpies and heat capacities at constant pressure (X. Daura and W.F. van Gunsteren, in preparation). There are two aspects of the results which I wish to discuss here. The first one is that, for the temperature range studied (298–360 K, with 10 K intervals) the higher the temperature the more favorable the (system) enthalpy is to folding. Since the free enthalpy of folding increases with temperature, the entropy must counteract the enthalpy trend. The second refers to the contribution of different potential energy terms to folding: internal (peptide) bonding interactions, internal non-bonding interactions and solvent–solvent interactions favor folding at all temperatures, while peptide–solvent non-bonding interactions strongly disfavor folding. While this is not unexpected, it called our attention to the fact that the contribution of solvent–solvent interactions to folding is similar in magnitude to the contribution of the peptide’s internal non-bonding interactions. It goes without saying that these results may not be extendable to peptides in water.

4 Outlook

There are three choices implicit in any MD simulation of peptide folding.

4.1 Type of degrees of freedom

The atomic representation of peptide and environment will probably take the lead in peptide folding studies in the coming years. Quantum dynamics will be out of question for a long while, and it is not even clear that quantum effects (non-accountable classically) may play an important role in peptide-folding dynamics. Simple models seem, with current methods and computational performances, an unnecessary reduction in regard to peptide folding. Implicit-solvent models, together with an atomic representation of the peptide, may be used, instead, to explore the long time limit.

4.2 Force field

The force field has been, traditionally, a cause of distrust in classical MD. Starting with the second-generation force fields already mentioned, important progress has been made [134–137]. Long-range interactions (e.g., Ewald-type sums or reaction field corrections for electrostatics and long-range cutoffs or corrections for van der Waals) have been, in general, already incorporated in the parametrization procedures.

Nevertheless, there is still work for force-field developers [138–142]. Water models with three interaction sites have been proven difficult to improve [143]. TIP5P [144, 145] is currently the best water model available, but is somewhat inconsistent with the peptide description and is computationally expensive. Polarizability has been long claimed to be the key addition to classical force fields. Although polarizable biomolecular force fields already exist [146–149], they require an additional computational effort and have not yet shown an unquestionable advantage over current non-polarizable ones (even for water).

Half-way between the sampling algorithm and the force field, pH stands as one of the missing parameters in standard MD. The pH is usually taken into account in an average way by fixing the protonation state of the titratable groups according to standard pK_A values. This is, however, a rather crude approximation, especially because pH is known to strongly affect folding. There exist a number of constant-pH algorithms, both for explicit-water [150–152] and implicit-water [153–155] MD simulations, but their properties have not been thoroughly investigated yet. In addition, they have an extra computational cost which has probably contributed to restrict their range of application so far.

4.3 Sampling of conformational space

Two recently implemented techniques, replica-exchange MD and parallel-replica MD, permit already the study of folding thermodynamics and kinetics, respectively, for reasonably sized polypeptides. Standard MD is still unique in that it delivers both types of information for free. Its timescale limitations are, however, frustratingly obvious. Nevertheless, ensemble-type simulations – many, very long (for current standards) simulations – of peptides in explicit solvent may be within reach in only a few years. The GRID initiatives may decisively contribute to it (<http://gridcafe.web.cern.ch/gridcafe/>).

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